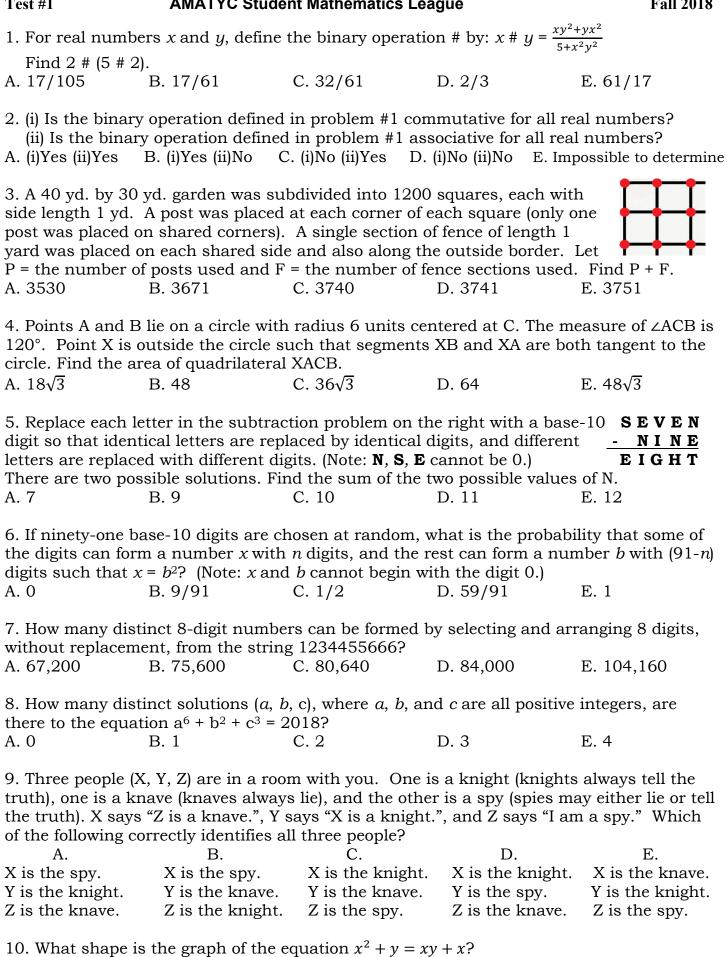
AMATYC Student Mathematics League



D. A parabola

E. Two lines

A. A hyperbola B. A line C. A hyperbola and a line

11. Every so often, a peculiar professor buys <i>n</i> snacks at the store and then arranges them in a circle. He eats one snack each day and gives the last one remaining to his dog. He begins at the top of the circle (#1), and then, moving clockwise, eats <i>every other</i> snack remaining on the table. For example, if he buys 5 snacks, he eats #1, skips #2, eats #3, skips #4, eats #5, skips #2, eats #4, then gives #2 to his dog. If he buys 125 snacks, which one will his dog eat?				
A. #122	_	C. #80	D. #64	E. #2
12. The solution tA. $0 < x \le 1$	to the equation (log B. $1 < x \le 10$	$(s_8 x^2)(\log_x 8)^2 = 1 \text{ sa}$ C. $10 < x \le 50$		
	emainder when 1! greater than 1 such B. 7		are of an integer.	
intercepts $(p, 0)$ a	By = 1 passes thro nd (0, q). If $p + q =$ B14/45	= 14, find A + B.		-
15. The roots of a rand s . If $\frac{r}{1+r}$ and A . $\frac{b-c}{a-b+c}$	$x^{2} + bx + c = 0, \text{ whe}$ $\frac{s}{1+s} \text{ are the roots } c$ $B. \frac{b-c}{b-a+2c}$	ere a , b , and c are of $x^2 + dx + e = 0$ (d) $C. \frac{3c-b}{a-b+c}$	real numbers with a , e are real), find a D. $\frac{3c-b}{b-a+2c}$	a nonzero, are $a + e$. E. $\frac{b+c}{b-a+2c}$
16. Two circles with the same center create a ring. A chord of the outer circle tangent to the inner circle has length $2\sqrt{19}$. The difference of the two circles' radii is 1. What is the greatest number of circles tangent to both the inner and outer circles that can fit inside the ring without overlapping?				
A. 57	B. 58	C. 59	D. 60	E. 61
17. Let P be the largest prime number that divides all four-digit numbers with identical digits (of the form $aaaa$). Let K be the y-coordinate of the vertex of the parabola with x-intercepts of $(2 \pm \sqrt{3}, 0)$ and a y intercept of $(0, -3)$. Find P + K.				
A. 110	\pm $\sqrt{3}$, 0) and a y in B. 103	C. 100	D. 99	E. 92
18. The first three terms of an arithmetic sequence are represented by $8x - 1$, $4x + 2$, and $2x - 6$. Find the sum of these three terms.				
A19	B11/2	C. 11/2	D. 19	E. 72
19. Emily drives to school at a speed of 60 miles per hour. On the return trip, she runs into traffic and travels at 20 miles per hour. What is her average speed for the entire trip?				
A. 24 mph	B. 30 mph	C. 36 mph	D. 40 mph	E. 42 mph

20. Three fair six-sided dice are rolled. Let P₁ be the probability that the sum of the numbers shown on the dice is 5. A different six-sided die is biased so that P(1) = P(2), P(3) = 2P(1), P(4)= 3P(2), P(5) = 4P(3) and P(6) = 3P(5). Let P_2 be the probability of rolling a 2 on this die. Let P₃ be the probability that a randomly selected integer between 1 and 999 inclusive is divisible by 39. Order these probabilities from greatest to least.

A. P₁, P₂, P₃

B. P₁, P₃, P₂

C. P₂, P₁, P₃

D. P₂, P₃, P₁

E. P₃, P₁, P₂